

Not A, but B

a.) $M_{V,A} = 1.4$

$M_{V,B} = 11.4$ (100x is 5 mags,
OR calculation via Eq. 3) (1 pt)

$m - M = 5 \log \left(\frac{d}{10 \text{ pc}} \right)$ (0.5 pt)

$d = 2.6 \text{ pc}$

\Rightarrow

$m - M = -2.9$ (0.5 pt)

$\Rightarrow m_{V,B} = 8.5$ (1 pt)

c $d = \left(\frac{1}{p''} \right)$

(0.5 pt)

$p'' = \frac{1}{2.6} = 0.38 \text{ arcsec}$

$= 1.1 \cdot 10^{-4} \text{ degree}$

(0.5 pt)

Two galaxy clusters

$$2\langle KE \rangle + \langle PE \rangle = 0$$

virial theorem

0.5 pt

$$PE = -\frac{GMm}{R}$$

0.5 pt

$$KE = \frac{3m\sigma_r^2}{2}$$

0.5 pt

⇓

if v is used instead of $3\sigma_r^2$ these 0.5 pt are not given but rest can be correct

$$M = \frac{3\sigma_r^2 R}{G}$$

0.5 pt

R & G are the same 0.5 pt

$$\sigma_{R \text{ coma}} = 3 \sigma_{R \text{ Fornax}}$$

$$\Rightarrow M_{\text{coma}} = 3^2 M_{\text{Fornax}}$$

$$X = 9$$

0.5 pt

One and one

a.) $F_{\text{tot}} = 1.25 \cdot F_{\text{bright}}$

1 pt

0.5 pt
formula

$$M_{\text{tot}} - M_{\text{bright}} = -2.5 \log_{10}(1.25)$$
$$= -0.24 \text{ mag}$$

0.5 pt
answer

b.) $\left(\frac{L}{L_{\odot}}\right) = \left(\frac{T}{T_{\odot}}\right)^4 \left(\frac{R}{R_{\odot}}\right)^2$

0.5 pt

$$\Rightarrow \left(\frac{L_1}{L_2}\right) = \left(\frac{T_1}{T_2}\right)^4 \left(\frac{R_1}{R_2}\right)^2$$

$$\Rightarrow \frac{R_1^2}{R_2^2} = \left(\frac{L_1}{L_2}\right) \cdot \left(\frac{T_2}{T_1}\right)^4$$

0.5 pt

surface
dist = πR^2

$$= 0.25 \cdot \left(\frac{1}{0.8}\right)^4$$

0.5 pt

$$= 0.61$$

↳ 61%

0.5 pt